

The 1998 Miyako fireball's trajectory determined from shock wave records of a dense seismic array

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A high velocity passage of a meteoroid through the atmosphere generates a shock wave with a conical front. When the shock front arrives at the surface, it causes high frequency ground motions that are registered on the seismograms. We can use seismological data to determine the trajectory of the meteoroid in the atmosphere. A strong shock wave from the 1998 Miyako fireball is recorded by more than 20 stations in a dense array of seismographs installed in the northeastern region of Honshu Island, Japan. We determine the velocity and the trajectory of the fireball in the upper atmosphere using the arrival times of the shock wave at the stations.

Key words: Shockwave, fireball, trajectory, seismic array.

1. Introduction

Meteoroid impacts into the Earth's atmosphere have been studied using various instruments. Ground-based camera video recorders networks have been widely used to observe fireballs and bolides (Halliday *et al.*, 1996). Recently, satellite-based optical instruments demonstrate their ability to register bolides in the atmosphere (e.g., Brown *et al.*, 2002). Barometer or infrasonic microphone arrays deployed on the surface are also effective systems to identify large bolides in the atmosphere (McIntosh *et al.*, 1976; ReVelle, 1976, 1997).

Another method to study features of fireballs and bolides is a seismological approach. Meteoroids with super-sonic velocities and bolides generate shock waves in the atmosphere. If the shock waves are sufficiently strong, they generate impulse ground motions that can be recorded by seismographs on the ground (Nagasawa, 1978; Nagasawa and Miura, 1987; Cevolani, 1994). Therefore, a dense array of seismographs installed for a purpose of monitoring earthquake activities is also a good apparatus for the fireball observations. Kanamori and his colleagues have demonstrated the ability of the seismic records to determine the trajectory of high velocity objects, space shuttles (Kanamori *et al.*, 1991; Mori *et al.*, 1991).

The bright 1998 Miyako fireball flew over a dense seismographic array deployed in the Tohoku region in Japan. The shock wave signals are clearly recorded on many seismograms of the array. The data provide a good opportunity to show a potentiality of a seismic array as a fireball observation system. In this page we report the determination of trajectory and velocity of the fireball by the analysis of the seismograms obtained by the array.

2. The Miyako Fireball and a Seismic Array

The bright Miyako fireball appeared at 3:20 am (the local time JST = UT + 9h) on March 30, 1998 in the northeastern region of the Honshu Island of Japan. The fireball was observed by an amateur astronomer's fireball patrol camera network. The visual magnitude was estimated to be -14 from the photograph records and the trajectory parameters were obtained by an analysis of two photos (Japan Fireball Network, 1998). It traversed across northeast Honshu Island from WSW to ENE with a velocity of about 19 km/sec. No meteorite related to the fireball has been recovered. The meteoroid likely fell onto the Pacific Ocean off the east coast of the region.

The fireball crossed the sky just above a dense seismic array, which was temporary installed by a consortium of seismological researchers from Japanese universities (the 1997–98 joint seismic observation in the Tohoku Backbone Range). Including permanent seismic stations that were installed by Tohoku University and the Japan Meteorological Agency, the array comprises 85 stations in an area of $4.0 \times 104 \text{ km}^2$ (Fig. 1). The main purpose of the seismic observation is to determine the source locations of microearthquakes in the region. The seismographs are very sensitive to the ground motions and their clocks are precisely maintained (10^{-6} sec) using GPS signals. The seismographs are deployed at selected locations where the background noise of the Earth, microtremors, is small. Almost all stations are installed on the surface and are sensitive to ground surface motions generated by a shock wave from the atmosphere.

3. Data

We inspect the seismic array data around the time of the fireball appearance. A shock wave arrival is easily noticed on a velocity seismogram by its characteristic waveform.

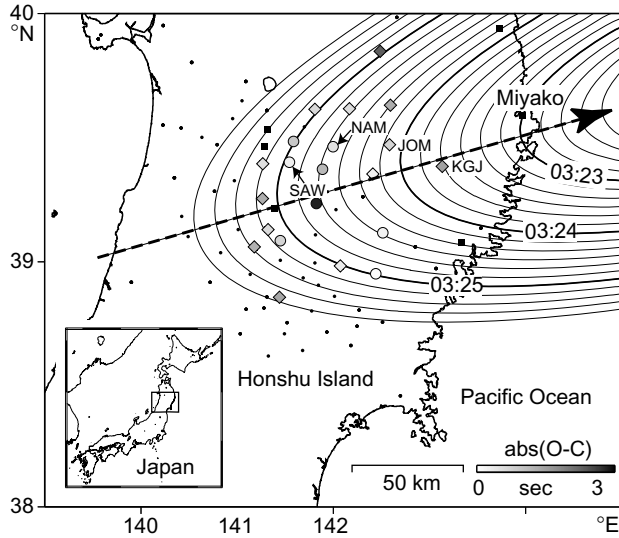


Fig. 1. Calculated isochronal lines of the shock wave arrivals. The arrow indicates the determined trajectory of the Miyako fireball. Diamonds are seismic stations at which observed arrival times are faster than calculated ones. Circles are seismic stations at which recorded observed arrival times are slower than calculated ones. The gray scale indicates the absolute value of the residual, the observed time minus the calculate time. Squares are seismic stations at which we observe unclear shock wave and are not used in the analysis. Dots are seismic stations which we observe no shock wave signals.

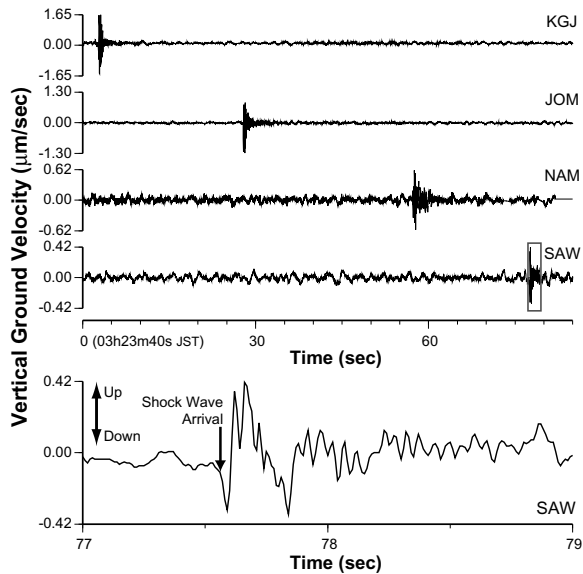


Fig. 2. Examples of shock waves, recorded at seismic stations, KGJ (39.3865°N, 141.5659°E, 375 m), JOM (39.4730°N, 141.2923°E, 210 m), NAM (39.4678°N, 140.9979°E, 245 m) and SAW (39.4030°N, 140.7720°E, 280 m). The lowermost seismogram shows the enlarged view of the part of shock wave signal at the SAW station. Note that the velocity seismogram of the vertical ground motion shows a N-shaped waveform. The negative represents downward motion. The shock wave signal necessarily begins with a downward motion. The reference time is 03h23m40s JST.

The shock wave generated by a meteoroid is a compressional shock wave followed by a rarefactional shock wave. The compressional and rarefactional shock waves cause the rapid downward and upward ground motions, respectively. These successive ground motions are recorded as a shape of

Table 1. List of seismic stations that detected shock wave signal.

Station	Latitude [°]	Longitude [°]	Height [m]	Arrival Time [h:m:s]
MYK	39.590	141.98	120	03:23:08.27
KGJ*	39.387	141.57	375	03:23:42.74
JOM*	39.473	141.29	210	03:24:07.83
MNS*	39.355	141.20	65	03:24:13.78
JOJ	39.080	141.67	180	03:24:19.71
JTH	39.939	141.86	200	03:24:21.96
NTM*	39.632	141.30	311	03:24:22.06
THR*	39.118	141.26	165	03:24:28.93
NAM*	39.466	141.00	245	03:24:37.34
HAN*	39.374	140.94	300	03:24:38.35
GTO*	39.237	140.91	610	03:24:41.29
YHB*	39.618	141.08	300	03:24:43.85
SAW*	39.403	140.77	280	03:24:57.55
JMK*	38.952	141.22	70	03:24:59.12
SWU*	39.486	140.79	445	03:25:01.14
HRQ*	38.984	141.04	123	03:25:01.50
WNS	39.278	140.82	280	03:25:02.32
OSK*	39.616	140.90	270	03:25:03.98
HMK*	39.848	141.24	650	03:25:06.76
KT44*	39.086	140.72	400	03:25:07.38
SNN	39.214	140.70	270	03:25:08.01
HRN*	39.256	140.63	170	03:25:08.64
KT43*	39.130	140.66	280	03:25:09.76
JRG*	39.396	140.63	200	03:25:12.09
NNW	39.466	140.64	170	03:25:16.46
KT48*	39.061	140.59	235	03:25:20.42
NKS	39.536	140.66	170	03:25:22.15
GNV*	38.857	140.72	440	03:25:39.11

*21 stations used for the analysis.

a reversed N on a velocity seismogram (Fig. 2). We identify shock wave signals from the fireball at 28 seismic stations (Table 1). At the other stations in the array, the shock wave signals are thought to be smaller than the background noises. The maximum observed ground velocity induced by the shock wave is 1.65×10^{-6} m/sec. We use here shock wave arrival times of 21 stations which record clear onsets of the signals. The arrival times of the shock wave are picked out with an accuracy of 0.1 seconds or less.

4. Method

To determine the trajectory, we make two approximations (1) that the fireball linearly penetrates through the atmosphere with a constant velocity v , and (2) that the shock wave speed c is uniform in the atmosphere and to be 320 m/sec. The first approximation is based on observations that meteoroids have nearly constant velocities in the upper atmosphere (e.g., Brown *et al.*, 2002; Halliday *et al.*, 1981). The second approximation is adopted because of small incident angles of the shock waves analyzed in this study. In the real atmosphere below a height of about 100 km, the shock wave speed may change in a range of 290 m/sec to 340 m/sec. However, the speed varies with the height. If the shock wave is propagated nearly vertically, the ray is hardly refracted and an average velocity can be used to calculate a travel time.

Table 2. Search domain, grid interval and optimum value of each parameter*.

Parameter	Search Domain	Grid Interval	Optimum Value and Confidence Interval	Photo Analysis Value
v [km/sec]	11~45	1.0	18 +7/-3	18.6
x_0 [km]	-110~-50	1.0	-93 +3/-3	—
y_0 [km]	180~250	1.0	207 +3/-2	—
γ [°]	270~300	0.5	287 +1/-1	296
θ [°]	10~40	0.5	18.5 +0.5/-0.5	18.3
t_0 [sec]	0~80	1.0	48 +3/-3	—

*The origin is (39°N, 141°E, 0) at 03h20m00s JST (UT + 9h).

Since the incident angles of the shock waves to almost all the stations used here are smaller than 30 degree, the errors caused by the second approximation are small compared with other practical uncertainties (Tatum, 1999).

For the case of a linear-motion of a meteoroid with a constant velocity, the generated shock wave front forms a cone; the isochronal curves of the shock wave arrival times on a flat surface are conic sections. While the meteoroid moves with a super-sonic speed (about 20 km/sec), the velocity of the shock wave is low, 320 m/sec. Then the semi-vertical angle of the shock wave cone is very small (about 1 degree). This angle is generally smaller than the angle of elevation of the meteoroid trajectory. Therefore the isochronal curves of arrival times on the surface are half ellipses in most cases.

We define two rectangular coordinate systems, (x, y, z) and (X, Y, Z) (Fig. 3). The origin of the coordinate (x, y, z) is given at a point on the Earth's surface. In this study the origin is at a point 39°N and 141°E. The x - y plane is a tangent plane of the Earth's surface at the origin. The x , y , and z axes point southward, eastward, and upward, respectively. The second set of coordinates (X, Y, Z) is introduced to describe the shock wave cone. Its origin is located at a point where the meteoroid trajectory intersects the x - y plane. The Z axis points in the direction of the approaching meteoroid. The X axis is on a vertical plane containing the trajectory. The Y axis is on the x - y plane and perpendicular to the X and Z axes. In such coordinate systems, the shock wave front and the trajectory of the fireball can be expressed as follows (Nagasawa and Miura, 1987).

$$\frac{\sqrt{X^2 + Y^2}}{\tan \beta} - Z = v(t - t_0) \quad (1)$$

$$\sin \beta = c/v \quad (2)$$

$$\begin{pmatrix} X \\ Y \\ Z \end{pmatrix} = \begin{pmatrix} \cos \gamma \sin \theta & \sin \gamma \sin \theta & -\cos \theta \\ -\sin \gamma & \cos \gamma & 0 \\ \cos \gamma \cos \theta & \sin \gamma \cos \theta & \sin \theta \end{pmatrix} \begin{pmatrix} x - x_0 \\ y - y_0 \\ z \end{pmatrix}, \quad (3)$$

where, v is the velocity of the meteoroid, γ is the azimuth of the trajectory (counterclockwise from the x -axis), θ is the elevation angle of the trajectory from the x - y plane, the point $(x_0, y_0, 0)$ is the intercept of the trajectory to the x - y plane at an expected time t_0 . The stations locations are converted from the geographic coordinates (the latitude, the longitude, the height) to the x , y , and z coordinates.

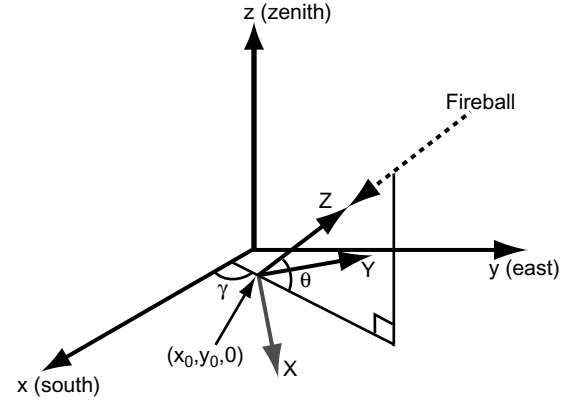


Fig. 3. Coordinate systems for the fireball trajectory used in the analysis.

Given a set of six parameters of the trajectory, v , γ , θ , x_0 , y_0 , t_0 , we can calculate the expected arrival time t_i at the i -th station whose coordinates are (x_i, y_i, z_i) . Let τ_i be the observed arrival time at the i -th station. The best set of the parameters can be retrieved by minimizing the sum of squared residuals $(t_i - \tau_i)^2$. However since there are many local minima of the sum in the six parameters space, the solution estimated by an inversion method easily falls into such local minima near the initial values. In order to find the best set of the parameters in the relevant space, we use a grid search method. The search ranges and the grid intervals of the individual parameters are summarized in Table 2. The 68.3% confidence interval of each parameter is estimated using the χ^2 test of the sum of the squared residuals.

5. Results and Discussion

The best six parameters for the trajectory and their confidence intervals are listed in Table 1. Parameters given by an analysis of photographic data (Japan Fireball Network, 1998) are also listed in Table 2. The trajectories determined by both the methods agree well with each other.

In Fig. 1 the projection of the fireball trajectory to the surface is drawn, with calculated isochrones of the shock wave arrivals. As shown in the figure, there is good the azimuthal coverage of the stations to determine the fireball trajectory. The calculated arrival times of the shock waves at the individual stations are consistent with the observed ones. The root mean square σ of the differences between the observed and calculated arrival times is 1.1 seconds. The semi-vertical angle of the shock front cone is smaller ($\beta \approx 1^\circ$) than the incident angle ($\theta = 18.5^\circ$). Therefore, the isochrones of the shock wave arrivals are half ellipses (Fig. 1). The arrivals of the shock wave begin at eastern stations, which are near the end point of the fireball trajectory, and retrograde westwards (Fig. 2). Such retrogression of the wave arrival is also caused by the slow shock wave velocity. The longest travel times that are observed at western stations are about 290 sec. These values correspond to travel distances of about 90 km. This means that the shock wave generation started at least from a height of more than 80 km, which coincides well with the reported height (86 km) at which the fireball started to emit light (Japan Fireball Network, 1998).

In this analysis we assume that the shock wave velocity is

uniform from the surface to the height of the fireball. However, the real atmosphere is apparently much more complex and there are spatial variations of the velocity with different spatial scales. The arrival time residuals whose r.m.s. $\sigma = 1.1$ sec, reflect such variations. Random components in the velocity variations do not greatly affect the estimation of the trajectory, since their effects averaged together by using many stations. However, there may exist systematic variations of the shock wave velocity that are neglected in the estimation. One potential source of error is the difference between the assumed and the real average velocities of shock wave. We adopt the average velocity of 320 m/sec in the analysis. The difference can be 20 m/sec or about 6% at most. The maximum difference may cause a discrepancy of a few km in the height and horizontal location between the real and the estimated trajectories.

Another important factor that is neglected in the analysis is the wind in the lower atmosphere. In particular the strong westerly wind, the jet stream, blows over the relevant latitudinal zone in the winter season. The shock waves are driven out of their travel paths that are expected for a still atmosphere. If the average westerly wind speed in the lower atmosphere with a representative thickness of 20 km is 20 m/sec at most, the eastward driven distance of the paths is about one km. This is within a range of the error for the trajectory estimation.

The results obtained in this analysis show that a dense seismic array is a useful system to observe fireballs. At present, there are about one thousand seismic stations in the Japanese islands, which extends for a length of about 2500 km. Many seismographs are installed on the ground or near the surface, and would be sensitive to the shock wave signals from fireballs. Data from the stations can be immediately transmitted to any laboratories in Japan through a communication satellite, enabling analyses of shock wave signals in real time. The seismic array can watch for fireballs 24 hours a day even through cloudy or rainy skies. It is expected that the seismic array can provide valuable data on fireball phenomena and the meteoroid flux rate.

6. Conclusions

We find clear shock waves records from the 1998 Miyako fireball in seismograms of a dense seismic array in the north-eastern Japan. We determine the trajectory of the fireball in the atmosphere from the arrival times of shock waves. In the calculation we assume that the fireball traverses linearly with constant velocity and a uniform shock wave speed of 320 m/sec in the atmosphere. The optimum values of the tra-

jectory parameters are the meteoroid velocity of 18 km/sec, the azimuth of the trajectory of 287° the incident angle of trajectory of 18.5° . We recommend a dense seismic array as a useful tool to observe fireball because of its independence of weather conditions and its potential for successful observations.

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