Is the plastic flow uniformly distributed below the seismogenic region?

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The cut-off depth of seismicity in and around the Nojima fault broken by the 1995 Kobe earthquake occurring in the intraplate Japan was compared with a brittle-ductile transition depth of the widely-accepted strength profile model of the crust. It was found that the cut-off depth is much deeper than the transition depth under the assumption that wet granite is deformed at a strain rate of $10^{-15}$/s. Such a small strain rate implies that the plastic flow is uniformly distributed below the seismogenic region. When the strain rate is assumed to be greater than $10^{-13}$, the cut-off depth can be attributed to the transition depth. This suggests that deformation is localized in a narrow fault zone below the seismogenic region even in the intraplate region.

1. Introduction

At present, the strength of the crust is understood based on a simple model which utilizes the friction law of rocks (Byerlee, 1978) in the shallower part of the crust (the brittle region) and the plastic flow law in the deeper part (the ductile region) (e.g., Kobayashi, 1977; Goetze and Evans, 1979; Brace and Kohlstedt, 1980; Kirby, 1980; Sibson, 1982). Important parameters of the flow law are temperature and strain rate. The strain rate assumed in the flow law is usually $10^{-14}$/s to $10^{-15}$/s for the intraplate region in the continental crust (e.g., Goetze and Evans, 1979; Brace and Kohlstedt, 1980; Kohlstedt et al., 1995). Such a small value of the strain rate implies that rocks are uniformly deformed in the ductile regime in the intraplate region.

However, it has been inferred from the postseismic deformation of large intraplate earthquakes that afterslips may occur on a downward extension of a seismogenic fault in the ductile region (e.g., Shen et al., 1994; Savage and Svarc, 1997). This inference suggests that deformation is localized even in the ductile region in an intraplate region. Although an alternative hypothesis asserts that the postseismic deformation is due to viscoelastic relaxation in the lower crust (e.g., Deng et al., 1998), this hypothesis might not be realistic because it requires the assumption of a viscosity much lower than that determined by another method (Kaufmann and Amelung, 2000).

The manner of deformation in the ductile region in the intraplate region has not yet been accurately elucidated. Even in the interplate region, a problem similar to that described above has been presented (Bourne et al., 1998). These phenomena are problematic because it is difficult for measurements at the surface to distinguish between the two deformation processes occurring in the deeper crust (Savage, 1990).

In this paper, we will infer the deformation process in an intraplate region from precise in-situ data obtained in the aftershock area of the 1995 Kobe earthquake. We will compare the cut-off depth of seismicity with a brittle-ductile transition depth estimated from an accurately estimated temperature profile, assuming various strain rates.

2. Cut-Off Depth of Seismicity

A vertical distribution of aftershock hypocenters of the 1995 Kobe earthquake is displayed in Fig. 1 (Nakamura and Ando, 1996). These hypocenters were calculated simultaneously with station corrections and a one-dimensional velocity structure by applying a joint hypocenter-velocity inversion program (Dietz and Ellsworth, 1990) to the data from a dense temporal network of 56 stations (Ohmi, 1995; Hirata et al., 1996). As is shown in Fig. 1, seismicity is confined to depths shallower than approximately 17 km except for a few events occurring beneath the main-shock hypocenter.

The standard error in focal depth was estimated as less than 0.3 km from rms P-arrival residuals of 0.06 s (Nakamura and Ando, 1996). However, focal depths could be shifted if the velocity structure was not accurately determined, given that a trade off exists between focal depth and velocity (Dietz and Ellsworth, 1990). The obtained velocity model was compared with that from a refraction seismic experiment (Piao et al., 1997) (see Fig. 1(b)). Since the velocities from the joint inversion are a little bit smaller than those from the refraction experiment, it is possible that the true cut-off depth is slightly deeper than the obtained one. Furthermore, station corrections are determined between −0.20 and 0.25 s in the joint inversion (Nakamura and Ando, 1996). Then, in the worst case, true P-arrival residuals for each station could be about 0.25 s. The P-arrival residuals correspond to an uncertainty in the cut-off depth of about 1.5 km. As a consequence, the cut-off depth is thought to fall between 15.5 and 18.5 km as hatched in Fig. 1(a). Although this is the cut-off depth of an aftershock distribution, we do not regard the cut-off depth as a temporal one, because microearthquakes...
occurred near the lower boundary of seismicity even before the Kobe earthquake (Kyoto Univ., 1995).

3. Temperature Profile

A temperature logging was conducted in the borehole drilled in granitic rocks down to a depth of about 2000 m from the surface through the Nojima fault, about six months after the drilling had been finished (Ikeda et al., 2001). Temperatures from the surface to a depth of 1100 m were measured without any disturbances by the drilling (Kitajima et al., 2001). Thermal conductivities and heat productions were also measured from a collection of core samples (Kitajima et al., 2001). Below 1100 m, temperatures were not measured because the borehole had been collapsed at a fracture zone of the Nojima fault. Given that the temperatures were measured in massive granitic rocks outside of the fracture zone, it is not likely that the measured temperatures were seriously affected by water circulation near the surface.

We estimated the temperature profiles from the surface to a depth of 30 km. The heat production, $A(z)$, is assumed to be distributed as $A(z) = A(0) \exp(-z/D)$ (Lachenbruch, 1970) where $z$, is the depth (m), $A(0)$ is the heat production at the surface, and $D$ is the width of the layer on which the radio isotopes are concentrated (m). The temperature, $T(z)$, is calculated as

$$T(z) = T_0 + \left( \frac{Q(0)}{K} - A_0 D / K \right) z + \left( A_0 D^2 / K \right) \left[ 1 - \exp\left( -z / D \right) \right],$$

where $T_0$ is the absolute temperature at the surface, $Q(0)$ is the heat flow at the surface, and $K$ is the thermal conductivity. We obtained the following values: $Q(0)$ of 56.6 (mW/m$^2$), $K$ of 1.22 to 3.09 (W/mK), and $A(0)$ of 1.1 to 2.0 ($\mu$W/m$^3$) (Kitajima et al., 2001). The value of $D$ was not estimated around the Nojima fault; it was assumed to be from 5 to 10 km in this study, following estimates of 7.8 km at the Hidaka, Japan region (Furukawa and Uyeda, 1986), and 10 km at the San Andreas (Lachenbruch, 1970). $A(0)$ was set as 1.0, 1.5, or 2.0 according to the obtained values. $K$ was set as 3.0, almost the upper limit of the obtained value, because values of $K$ showed a tendency to increase with bulk density (Kitajima et al., 2001).

Figure 2(a) shows four profiles for different combinations of parameter values of the heat production and the width of the layer on which radio isotopes are concentrated. Two extreme cases are also shown. The first extreme case is that
the heat production is constant independently of depth. The second is no heat production. The temperature at the cut-off depth was determined to be about 600 K except in these two cases.

4. Strength Profile

The stress difference $\sigma_1 - \sigma_3$ in the ductile regime is computed as

$$\sigma_1 - \sigma_3 = (\varepsilon/A \exp(-H/RT))^{1/n},$$

where $\varepsilon$ is the strain rate (s$^{-1}$), $A$ is a constant, $H$ is the activation energy, and $R$ is the gas constant (Goetze and Evans, 1979). $A$, $H$, and $n$ are set as $2.0 \times 10^{-4}$ (MPa$^{-2s^{-1}}$), 137 (KJmol$^{-1}$), and 1.9, respectively, following the values for wet granite (Hansen and Carter, 1982), and assuming that materials around the brittle-ductile transition are composed of granitic rocks (Shimada, 1993). The influence of usage of different flow laws on the result will be discussed later.

In the brittle region, the maximum compressional stress, $\sigma_1$ is calculated as

$$\sigma_1 = [(\mu^2 + 1)^{1/2} + \mu]/((\mu^2 + 1)^{1/2} - \mu)\sigma_3 - (2\mu((\mu^2 + 1)^{1/2} - \mu))p,$$

where $\sigma_3$ is the minimum compressional stress, $\sigma_1$ is the coefficient of friction, $p$ is the pore pressure (Jaeger and Cook, 1979). The shear stress $\sigma_3$ is calculated as,

$$\tau = ((\sigma_1 - \sigma_3)/2) \sin(\tan^{-1}(1/\mu))/2.$$  

In and around the Kobe aftershock region, it was known that the maximum compressional stress was aligned horizontally along the E-W direction, and that the magnitude of $\sigma_3$ is almost the same as the vertical stress (Iio, 1996). $\sigma_3$ is calculated then as $2.75 \times 10^{-2}$ z (MPa).

Figure 2(b) displays strength profiles in the brittle and ductile regions calculated from the temperature profiles obtained earlier. The pore pressure is assumed to be hydrostatic, $\mu$ is set as 0.6, and $\varepsilon$ is set as $3 \times 10^{-15}$ (s$^{-1}$). The shear strengths estimated from the Byerlee’s friction law and the flow law of wet granite (Hansen and Carter, 1982), and assuming that materials around the brittle-ductile transition are composed of granitic rocks (Shimada, 1993). The influence of usage of different flow laws on the result will be discussed later.

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where $\sigma_3$ is the minimum compressional stress, $\sigma_1$ is the coefficient of friction, $p$ is the pore pressure (Jaeger and Cook, 1979). The shear stress $\sigma_3$ is calculated as,
Next, we examined the parameter values used in the above calculation. Pore pressure, coefficient of friction, and/or strain rate can be a control parameter for strength models. Figure 3 shows modified strength profiles using different values for the above parameters. Pore pressure is assumed to be not only hydrostatic but also suprahydrostatic, and $2.4 \times 10^{-2} \times (\text{MPa})$. $\mu$ is set not only as 0.6 but also as 0.2, which values are estimated from numerous microearthquake focal mechanisms in the central Kinki district, Japan (Iio, 1997). Strain rate $\dot{\varepsilon}$ is changed from $3 \times 10^{-15}$ to $3 \times 10^{-14}$, $3 \times 10^{-13}$, and $3 \times 10^{-12}$, respectively. In all cases, $A(0)$ and $D$ are fixed to be the most likely values of 1.5 and 10, respectively.

A series of combinations of parameters can explain the cut-off depth: (1) $\dot{\varepsilon}$ of $3 \times 10^{-12}$ and $\mu$ of 0.6, (2) $\dot{\varepsilon}$ of $3 \times 10^{-13}$ and suprahydrostatic, and (3) $\dot{\varepsilon}$ of $3 \times 10^{-13}$ and $\mu$ of 0.2. These results clearly show that larger strain rates are necessary. When the Byerlee’s law is assumed, $\dot{\varepsilon}$ should be set as approximately $3^{-12}$.

Table 1 demonstrates strain rates computed from various fault widths and average slip rates, under the assumptions that faults below the seismogenic region slip at the same rate as those at the surface, and that fault width is constant in the ductile region. In Table 1, the faults are distinguished into three groups by their average geological slip rates (Research Group for Active Faults of Japan, 1980). It is necessary that the fault width be narrower than 100 m for all types of faults, for the purpose that the strain rate is set as greater than $3 \times 10^{-12}$. This suggests that below the seismogenic region, deformation is localized in a narrow zone even in an intraplate region, as schematically displayed in Fig. 4.

### 5. Discussion

#### 5.1 Flow law in the ductile layer

In the above, we estimated the strength in the ductile layer by the flow law of wet granite. P-wave velocities around the transition depth of 10 to 15 km are estimated as 6.0 or 6.2 km/s, as shown in Fig. 1(b). These values are consistent with laboratory measured velocities of granitic rocks (e.g., Holbrook et al., 1992). Consequently, rocks above a depth of 18 km are thought to be granitic. In some reports, a flow law of dry granite was used to explain the cut-off depth, because the dry flow law predicts a stronger strength than the wet flow law (e.g., Shimada, 1993). However, it is not likely that the region around the brittle-ductile transition is dry, since it is believed that the lower crust has significant water contents, particularly in the upper part (e.g., Jones, 1992). In Japan, high conductivity anomalies in the lower crust were found except the fore-arc region and it is inferred that the lower crust has high water contents (Utada et al., 1996).

#### 5.2 Brittle-ductile transition

A criterion for the brittle-ductile transition different from the one used in this study, the Goetze’s criterion, is also displayed in Fig. 3. That criterion is that the stress difference necessary for ductile flow is about equal to the confining pressure (Kohlstedt et al., 1995). The results are not seriously affected by the different criterion. The intersections of the line for the Goetze’s criterion and the flow law curves show almost the same depth as those of the lines of the Byerlee’s law.

The discrepancy between the cut-off depth and the brittle-ductile transition depth cannot be explained by a modified model of the strength profile having the semi-brittle (transitional) zone (Strehlau, 1986; Ohnaka, 1992). If the transition from the brittle to semi-brittle region were related to the cut-off depth, the introduction of the semi-brittle zone would make the cut-off depth shallower rather than deeper. On the other hand, if the transition from the semi-brittle to the ductile region were related to the cut-off depth, it would make the transitional depth slightly deeper due to a reduction of the frictional strength. However, the decrease in strength of the flow law immediately beneath the transition depth is so steep that the reduction of frictional strength does not seriously change the brittle-ductile transition depth. Consequently, the introduction of the semi-brittle behavior cannot explain the
observed cut-off depth of the seismicity.

Another hypothesis is that the cut-off depth is determined by the transition to the stable frictional sliding regime (Tse and Rice, 1986). It is estimated that the cut-off depth predicted by this idea is shallower than the depth of the transition to the plastic flow (Kohlstedt et al., 1995). Thus, in this case also, it is necessary to increase the plastic flow strength.

5.3 Applicability of experimental results

More fundamental questions have been raised about the application of experimental results to the estimate of the strength in the crust (Paterson, 1987; Chester, 1995). It is claimed that in the case of quartz-rich rocks, it is premature to attempt any extrapolation of the experimental results to geological conditions except as an upper bound of the plastic flow strength (Paterson, 1987). If the estimated plastic flow strength were only an upper bound, the discrepancy between the estimated brittle-ductile transition and cut-off depth would be more serious, and would be emphasized by a possible reduction of the plastic flow strength. In this case also, we have to introduce higher strain rates in order to overcome the discrepancy.

5.4 Deformation in the lower crust

When the deformation in the ductile region is localized in a narrow fault zone, the strain rate in the adjacent region is naturally lower than that of the fault zone. Then, if the flow law and its parameter values, excepting the strain rate, were the same in both regions, the adjacent region would be weaker than the fault zone. Thus, there should be differences in either the flow law or its parameters between the fault zone and the adjacent region. There are two possibilities to explain this sort of difference. The first is that water is localized in the fault zone (Kronenberg et al., 1990). The second is that grain sizes in the fault zone are smaller than those in the adjacent region (Bell and Etheridge, 1973).

6. Concluding Remarks

We found that the cut-off depth of seismicity in and around the Nojima fault broken by the 1995 Kobe earthquake is not explained by the wet granite strength model in which a distributed plastic flow is assumed below the seismogenic region. We showed that the cut-off depth could be explained by the assumption that the deformation is localized in a narrow zone of a downward extension of the seismogenic fault even in the intraplate region. This result was obtained only at one site, but it may be universal in the intraplate region given evidence that cut-off depths in other regions in the Japanese Island arcs also have a tendency to coincide with a depth of approximately 600K (Ito, 1990; Kitajima et al., 2001). This new scope is important in considering the deformation process of intraplate regions, and in understanding the generating process of intraplate earthquakes.

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